работ в послеаварийный период. Представленный анализ действий японской стороны и международных организаций по смягчению и ликвидации последствий аварии и известные результаты моделирования распространения радиоактивных продуктов в окружающей среде позволяют сделать важные шаги в понимании основных причин, уровней и последствий большой аварии на АЭС Fukushima-Daiichi. Полученные оценки носят предварительный характер и предполагают дальнейший мониторинг и анализ развития вопросов по обеспечению экологической безопасности и устранению последствий аварии на АЭС.

Ключевые слова: Фукусимская авария, экологические последствия, радиоактивные выбросы.

I.I. Kozlov. Analysis of ecological consequences and lessons of the Fukushima accident. The events that occurred at the nuclear power plant (NPP) Fukushima-Daiichi forced all the world nuclear community and government bodies of ecological safety regulation to return again, after Chernobyl accident, to the need of revaluing the safety of all operating and designed NPPs. The consequences connected with emissions of radioactive products to the environment increase the validity of studying and analyzing the environmental issues, while evaluating the works done in the postemergency period. The presented analysis of the actions of the Japanese side and of the international organizations on mitigation and elimination of consequences of the accident, as well as the results of modeling of radioactive products distribution in environment allow to take important steps in understanding the main reasons, processes and consequences of the big accident on the nuclear power plant Fukushima-Daiichi. The obtained estimates are preliminary and require further monitoring and analysis of issues on ecological security and elimination of consequences of accidents at NPPs.

Keywords: Fukushima accident; ecological consequences; radioactive emissions.

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DEFLAGRATION-TO-DETONATION TRANSITION AND THE DETONATION INDUCTION DISTANCE ESTIMATION

Introduction. Turbojet and turbofan engines at flight Mach numbers exceeding 3 are very expensive. In particular, pulse detonation engine (PDE) is more attractive energetically for flight Mach numbers of about 3…4 [1]. But in order to use detonations for propulsion and to realize the corresponding thermodynamic advantages (they lead to reduced fuel consumption) some problems must be resolved. These problems deal mainly with achievement and control of detonations in a propulsion device. Among these problems are [1]:
— necessity of low-energy source for the detonation initiation;
— knowledge of geometry of the combustion chamber to promote detonation initiation and survival at lowest possible pressure lost.

Both problems are related to fundamental problem of deflagration-to-detonation transition and calculating of the detonation induction distance. Calculating of the detonation induction distance (and the detonation wave formation time) is also very important for explosion safety. And yet there are no reliable analytical methods for such calculating.

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ENERGETIKA, TEPLOTEHNIKA, ELEKTROTEHNIKA
Literature review. Results of experimental researches for the deflagration-to-detonation transition (DDT) are summarized by Michael Nettleton [2]. The key ideas for physical and chemical mechanisms of transition from deflagration to detonation are described in book [3]. Multidimensional time-dependent solutions of the Navier-Stokes equations are used to study the processes leading to DDT in an energetic reactive gas mixture [4, 5]. Numerical simulations of DDT, obtained by Elaine Oran (US Naval Research Laboratory) and her co-authors [4, 5], describe the transition phenomena in details, e.g. the development of hot spots (ignition centers) and spontaneous reaction waves are investigated. But either these numerical solutions or others [6…8] need a lot of computer time. And it is not convenient for problems of the DDT control, i.e. for real-time computing (especially for the explosion safety control).

Research goal. Developing a mathematical model of DDT that leads to simple analytical estimates for the detonation induction distance (DDT run-up distance) and the detonation wave formation time (DDT time) without detailed phenomena consideration.

Research description. The reason of DDT is instability of laminar flames. Physical model for DDT contains the next stages:
— there exists a possibility of the laminar flame instability;
— as the result of two-dimensional (multidimensional) flame instability the flame front distortion and turbulent combustion take place;
— flame accelerates because of the burning-surface area increase [9];
— accelerating flame generates shock wave and detonation.

Solutions for the detonation induction distance \( X_d \) and the DDT time \( \tau \) are obtained by H. Jones and M. Nettleton [2] for different types of the flame acceleration \( g_f \). If \( g_f = \text{const} \), that is flame acceleration is constant, distance \( X_f \) between the point of ignition and the point, of flame positioning during the shock wave formation can be estimated as [2]

\[
X_f = \frac{2a_s^2}{g_f \beta_f^2 (\gamma_1 + 1)^2},
\]

where \( B_f = \text{const} \) \((0 < \beta_f \leq 1, \beta_f = 0,9 \ \text{in most cases})\);

\( a_s \) sonic speed for inflammable mixture;

\( \gamma_1 \) the ratio of specific heats for this mixture.

Distance \( X_s \) between the point of ignition and the point, where the shock wave is generated can be assessed as [2]

\[
X_s = \beta_f (\gamma_1 + 1)X_f,
\]

that is

\[
X_s = \frac{2a_s^2}{g_f \beta_f (\gamma_1 + 1)}.
\] (1)

For open spaces either wide channels and tubes with smooth walls [2]

\[
X_s \approx X_d.
\]

So to obtain of the detonation induction distance \( X_d \) (or \( X_s \)) formula it is necessary to estimate the flame acceleration \( g_f \).

Such estimate is based on the flame stability problem solution. This problem is solved for the flames propagating in open spaces through viscous incompressible environment [10]. The solution is enlarged to cylindrical tubes. Case of instability wave length \( \lambda_{m} \) for the fastest growth rate of perturbation amplitude is obtained [10].
Arc distance $l$ for the distorted flame, corresponding to $\frac{\lambda_m}{2}$ is

$$l = \int_{-\lambda_m/4}^{\lambda_m/4} \left[ 1 + \frac{\partial}{\partial y} (\text{Re} \varepsilon_1) \right]^2 dy,$$

where $\varepsilon_1(y, t) = A_0 h^{-1} \exp(ihy - i\omega t)$ flame leading edge perturbation;
- $h = 2\pi / \lambda > 0$ wave number;
- $\lambda$ wave length;
- $i$ unit imaginary number;
- $\omega$ complex number (eigen-value);
- $y$ spatial coordinate;
- $t$ time;
- $A_0$, arbitrary constant;
- $\text{Re} \varepsilon_1$, real part of $\varepsilon_1$.

The quantity $\left[ \frac{\partial}{\partial y} (\text{Re} \varepsilon_1) \right]^2$ is small [10]. So

$$l \approx \int_{-\lambda_m/4}^{\lambda_m/4} \left[ 1 + \frac{1}{2} \left( \frac{\partial}{\partial y} (\text{Re} \varepsilon_1) \right)^2 \right] dy,$$

and

$$l = \frac{\lambda_m}{2} + \int_{0}^{\lambda_m/4} \frac{\partial}{\partial y} (\text{Re} \varepsilon_1) \gamma dy. \quad (2)$$

It is obvious that for $\lambda = \lambda_m$

$$\text{Re} \varepsilon_1 = \lambda_m \cos \frac{2\pi y}{\lambda_m} \cos \frac{2\pi y}{\lambda_m} \exp \left( \frac{2\pi u_i t}{\lambda_m} \right),$$

where $z = -\frac{i\omega}{\lambda u_i}$ is dimensionless eigen-value [10];
- $u_i$ is laminar combustion velocity.

Let us assume

$$K = A_0 \exp \left( \frac{2\pi u_i t}{\lambda_m} \right). \quad (3)$$

Then

$$\int_{0}^{\lambda_m/4} \left[ \frac{\partial}{\partial y} (\text{Re} \varepsilon_1) \right]^2 dy = K^2 \int_{0}^{\lambda_m/4} \sin \frac{2\pi y}{\lambda_m} dy,$$

$$\int_{0}^{\lambda_m/4} \frac{\partial}{\partial y} (\text{Re} \varepsilon_1) \gamma dy = K^2 \left( \frac{\lambda_m}{2} \cos \frac{4\pi y}{8\pi} \sin \frac{4\pi y}{\lambda_m} \right)_{0}^{\lambda_m/4},$$

and finally

$$\int_{0}^{\lambda_m/4} \left[ \frac{\partial}{\partial y} (\text{Re} \varepsilon_1) \right]^2 dy = K^2 \frac{\lambda_m}{8}. \quad (4)$$
Substituting (4) into (2), we obtain
\[
l = \frac{\lambda_m}{2} \left( 1 + \frac{K^2}{4} \right).
\]

It is evident that
\[
\frac{l}{\lambda_m/2} = 1 + \frac{K^2}{4}.
\]

So the ratio of areas for the disturbed flame and the planar flame will equal
\[
\left( \frac{l}{\lambda_m/2} \right)^2 = \left( 1 + \frac{K^2}{4} \right)^2.
\]

By law of areas
\[
\frac{u_f}{u_l} = \left( 1 + \frac{K^2}{4} \right)^2,
\]

where \( u_f \) is the flame propagation velocity.

Quantity \( K \) is small. So
\[
u_f = u_l \left( 1 + \frac{K^2}{2} \right),
\]

and
\[
\frac{du_f}{dt} = u_l K \frac{dK}{dt}.
\]

Obviously the shock wave is generated when flame propagating velocity is close to the sonic speed \( a_i \) for initial inflammable mixture. Let us assume that such velocity can be reached within time \( \tau_f \). Then, due to (5)
\[
a_i = u_l \left( 1 + \frac{K^2(\tau_f)}{2} \right),
\]

\[
1 + \frac{K^2(\tau_f)}{2} = \frac{1}{M_i},
\]

and
\[
K^2(\tau_f) = \frac{2(1 - M_i)}{M_i},
\]

where \( M_i = \frac{u_i}{a_i} \) the Mach number.

Due to (3)
\[
\frac{dK}{dt} = \frac{2\pi u_i}{\lambda_m} K,
\]

so
\[
\frac{du_f}{dt} = \frac{2\pi u_i^2}{\lambda_m} K^2.
\]
and, in particular,

$$\frac{du_f}{dt}(\tau_s) = \frac{2\pi u_t^2}{\lambda_w^2} K^2(\tau_s).$$  \hspace{1cm} (7)

Substituting (6) into (7), we obtain

$$\frac{du_f}{dt}(\tau_s) = \frac{4\pi u_t^2(1-M_1)}{\lambda_w M_1}.$$  \hspace{1cm} (8)

Thus, at the moment when the flame propagating velocity is close to the sonic speed $a_1$, the flame is acceleration

$$g_f = \frac{4\pi u_t^2(1-M_1)}{\lambda_w M_1}.$$  \hspace{1cm} (8)

With regard to [10]

$$z_0 = \frac{\delta_2}{\delta_2 + 1} \left( -1 + \sqrt{\frac{\delta_2 + 1}{\delta_2} - 1} \right),$$

and

$$-\left( 1 + \frac{\delta_2}{\delta_2 + 1} z_0 \right) z_1 = z_0 \left[ \frac{1}{2} \left( 1 + \frac{z_0}{2} \right) (2\delta_2 + 1) + \left( \frac{\delta_2}{\delta_3} - 1 \right) + \delta_3^{-1} (\delta_3 + 1 + \frac{\delta_2 + 1}{\delta_3} z_0) \right] + \frac{1}{2} (\delta_2 - 1) \left( 1 + 2z_0 + \frac{z_0^2}{\delta_3} \right),$$

$$g_f = \frac{z_0^2 u_t^2 (1-M_1)}{2z_1 L M_1},$$  \hspace{1cm} (8)

where $\delta_2 = \frac{\rho_1}{\rho_2}$, $\rho_1$ is the initial inflammable mixture density, $\rho_2$ is density of combustion products;

$$\delta_3 = \delta_2 - \frac{1}{e};$$

$m = \text{const}$ exponent in dependence of dynamic-viscosity coefficient on temperature;

$L$ is the flame thickness.

Substituting (8) into (1), we obtain

$$X_s = -\frac{4z_1 L}{(1-M_1) M_1 x_0^2 B_f (\gamma_1 + 1)}. $$  \hspace{1cm} (9)

Formula (9) represents an is analytical estimate for the detonation induction distance.

For DDT time $\tau_s$ such approximate estimate will be:

$$\tau_s = \frac{X_s}{u_t}. $$  \hspace{1cm} (10)

Thus the analytical estimates for DDT run-up distance and for the detonation wave formation time are obtained. Calculation these algebraic formulae is very simple requiring a minimal computer time, but such calculating does not describe the deflagration-to-detonation transition phenomena and its nature in detail.

**Results.** To verify the proposed mathematical model the calculations of the detonation induction distance $X_s$ and of DDT time $\tau_s$ have been implemented for different combustible environments. The results are given in Table.
Detonation induction distance $X_s$ and DDT time $\tau_s$ for different combustible media

<table>
<thead>
<tr>
<th>Combustible medium</th>
<th>$X_s$</th>
<th>$\tau_s$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gas mixtures near stoichiometry</td>
<td>10 mm...50 cm</td>
<td>0.001 s...5 s</td>
</tr>
<tr>
<td>Gas mixtures near concentration combustion limits</td>
<td>50 cm...5 m</td>
<td>5 s...15 s</td>
</tr>
<tr>
<td>Fine-dyspersated aerosols and dust suspensions</td>
<td>1 m...10 m</td>
<td>5 s...1 min</td>
</tr>
<tr>
<td>Aerosols and dust suspensions</td>
<td>5 m...15 m</td>
<td>15 s...2 min</td>
</tr>
<tr>
<td>Aerosols and dust suspensions near concentration limits</td>
<td>more than 15 m</td>
<td>more than 2 min</td>
</tr>
</tbody>
</table>

Those results are in good agreement with experimental data for open spaces, wide channels and wide tubes with smooth walls. It is well known [2] that wall roughness and obstacles in channels and tubes do significantly reduce DDT run-up distance and DDT time (in some cases in several times, up to 20...50 times).

Conclusions. Main conclusions of research effected are the following:
- the mathematical model for DDT is based on the flame stability problem solution;
- simple algebraic formulae for estimates of the detonation induction distance (9) and DDT time (10) are obtained;
- formula (9) for the detonation induction distance estimate is useful for PDE designing and for explosion proof projecting;
- formula (10) for DDT time first of all amplifies mathematical support of the automated control systems for the potentially explosive objects;
- due to (9) the detonation induction distance for slow-burning mixtures is much more than for fast-burning mixtures, because this distance is directly proportional the flame thickness $L$ and inversely proportional Mach number $M_1$.

Literature / References


АНОТАЦІЯ / ANNOTATION / ABSTRACT

В.Е. Волков. Перехід горіння в детонацію та оцінка довжини переддетонаційної ділянки. Перехід горіння в детонацію є цікавим як з точки зору вибухобезпеки, так і для проектування імпульсних детонаційних двигунів. Такі
V.E. Volkov. Deflagration-to-detonation transition and the detonation induction distance estimation. Deflagration-to-detonation transition is interesting both for explosion safety and for the pulse detonation engine designing. Such engines are energetically favorable at flight Mach numbers exceeding 3. But transition from subsonic combustion to detonation is not investigated enough at present, and that is a serious difficulty both to the explosion safety problem solution and to engineering of detonation engines (both aeroengines and rocket engines). The aim of the study is investigation of mathematical laws for the mentioned transition. A mathematical model for deflagration-to-detonation transition that is based on the solution of the flame stability problem is offered. This model amplifies modern theory of combustion and explosion and turbulence theory. Theoretical estimates for the detonation induction distance and for the detonation wave formation time are made. It is proved that the detonation induction distance for a slow-burning mixture is greater than for a fast-burning one. The obtained results make it possible to improve mathematical support of the automated control systems for the dangerously explosive objects and the detonation engine designing.

Keywords: deflagration, detonation, instability, mathematical model, detonation induction distance.

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